

# Optics: gain/absorption calculation

There are two different kind of gain/absorption calculations which can be made in nextnano.NEGF:

- the semiclassical one uses the populations and the linewidths calculated from the NEGF steady-state solution to calculate the gain/absorption in a semiclassical way;
- linear response theory to an a.c. incoming field. In this case, time-dependent Green's functions are considered.

## Semiclassical gain/absorption calculation

From the Green's functions calculated in steady-state, the populations are extracted in the Wannier-Stark basis. The linewidths are also calculated in this basis. The semiclassical gain/absorption spectrum is then calculated according to:

$$g(\hbar\omega) = \sum_{i \neq j} (\rho_j - \rho_i) \sim d_{ij}^2 \sim \frac{\Gamma_{ij}}{(\hbar\omega - E_{ij})^2 + \Gamma_{ij}^2/4} \frac{e^2}{\epsilon_0 \sqrt{\epsilon_r}} \sim c$$

where

- $\rho_i$  is the electron density in the state  $i$ .  $\rho_i = p_i \sim n_{3D}$  where  $p_i$  is the normalized population in state  $i$  and  $n_{3D}$  the averaged 3D electron density.
- $E_{ij} = E_j - E_i$  is the transition energy between states  $i$  and  $j$
- $d_{ij}$  is the dipole of the transition.  $d_{ij} = \int dz \sim \psi_j(z) \sim z \sim \psi_i(z)$ .
- $\Gamma_{ij}$  is the linewidth (full half at half maximum) of the transition calculated from the NEGF steady state
- $\epsilon_r$  is the relative permittivity
- $\epsilon_0$  is the vacuum permittivity
- $e$  is the elementary charge.

## Gain/absorption calculation from linear response theory to an a.c. field

In this case the perturbation due to an a.c. electric field along  $z$  is considered. The perturbing Hamiltonian reads in the Lorenz Gauge:  $H_{ac} = e \sim z \sim E e^{-i\omega t}$  where the amplitude  $E$  of the electric field is small and can be considered as a perturbation. The response Green's function  $\delta G^<(E, \omega)$  is calculated within linear response theory. As shown by Wacker (Phys. Rev. B 66, 085336 (2002)), the Green's function linear response reads:  $\delta G^R(E, \omega) = G^R(E + \hbar\omega) (H_{ac} + \delta \Sigma^R(E, \omega)) G^R(E)$

$\delta G^<(E, \omega) = G^R(E + \hbar\omega) H_{ac} G^<(E) \parallel + G^<(E + \hbar\omega) H_{ac} G^A(E) \parallel + G^R(E + \hbar\omega) \delta \Sigma^R(E, \omega) G^<(E) \parallel + G^R(E + \hbar\omega) \delta \Sigma^<(E, \omega) G^A(E) \parallel + G^<(E + \hbar\omega) \delta \Sigma^A(E, \omega) G^A(E)$   
In the self-consistent gain calculation, the 3 last terms are accounted. Indeed, to account for them, the self-energies  $\delta \Sigma(E, \omega)$  need to be calculated from  $\delta G^<(E, \omega)$ , requiring a self-consistent loop.

From this Green's function response, the a.c. conductivity is calculated:

## Permittivity and gain/absorption

The bulk relative permittivity, or dielectric constant, is assumed to be given by the [Lyddane-Sachs-Teller relation](#):

$$\epsilon_{\text{bulk}}(\omega) = \epsilon_{\infty} + (\epsilon_{\infty} - \epsilon_{\text{static}}) \frac{\omega_{\text{TO}}^2}{\omega^2 - \omega_{\text{TO}}^2}$$

In the self-consistent gain calculation, the quantity which is actually calculated is the a.c. conductivity  $\sigma(\omega)$ .

The complex relative permittivity which is output is then:

$$\epsilon_{\text{r}}(\omega) = \epsilon_{\text{bulk}}(\omega) - i \frac{\sigma(\omega)}{\omega \epsilon_0}$$

Finally the gain reads

$$g(\omega) = -\frac{\text{Re}(\sigma(\omega))}{\epsilon_{\text{r}}(\omega)}$$

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