Optics: gain/absorption calculation

There are two different kind of gain/absorption calculations which is given by nextnano.NEGF:

- the semiclassical one, which uses the populations and the linewidths calculated from the NEGF steady-state solution to calculate the gain/absorption in a semiclassical way;
- the "self-consistent" one, fully calculated using the NEGF formalism. In this case, linear response theory to an a.c. incoming field is considered, and time-dependent Green's functions are used.

Semiclassical gain/absorption calculation

From the Green's functions calculated in steady-state, the populations are extracted in the Wannier-Stark basis. The linewidths are also calculated in this basis. The semiclassical gain/absorption spectrum is then calculated according to:

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$$ g(\hor \omega_{ij}^2 \sim \frac{ij}^2 \sim \frac{ij}^2 \sim \frac{ij}^2 + \frac{ij}^2 + \frac{ij}^2 + \frac{ij}^2 \sim \frac{ij}^2 + \frac{i
```

where

- \$\rho_i\$ is the electron density in the state \$i\$. \$\rho_i = p_i ~ n_{3D}\$ where \$p_i\$ is the normalized population in state \$i\$ and \$n_{3D}\$ the averaged 3D electron density.
- \$E {ij} = E j E i\$ is the transition energy between states \$i\$ and \$j\$
- d_{ij} is the dipole of the transition. $d_{ij} = \int dz \sim psi_{j}(z) \sim z \sim psi_{i}(z)$.
- \$\Gamma_{ij}\$ is the linewidth (full half at half maximum) of the transition calculated from the NEGF steady state
- \$\epsilon r\$ is the relative permittivity
- \$\epsilon 0\$ is the vacuum permittivity
- \$e\$ is the elementary charge.

This semiclassical gain calculation has the following limitations:

- it depends on the choice of the basis (the Wannier-Stark basis is considered, but an other basis could be considered as well). Coherent terms are not considered, only populations.
- the linewidths are extracted at the Wannier-Stark energies, which might not be accurate as in the NEGF formalism they are energy dependent.
- the broadening is assumed to be Lorentzian, whereas in the NEGF treatment no assumption is made (non-Markovian treatment).

For the above reasons, the quantum treatment described below using perturbation theory is much more accurate.

Gain/absorption calculation from NEGF linear response theory

In this case the perturbation due to an a.c. electric field along \$z\$ is considered. The perturbating

Hamiltonian reads in the Lorenz Gauge: $\$\$ H_{ac} = e \sim z \sim \text{delta F} \sim e^{-i \text{omega t}} \$\$$ where the amplitude \$E\$ of the electric field is small and can be considered as a perturbation. The response Green's function $\$\delta G^{(E,\omega)}$ is calculated within linear response theory. As shown by Wacker (Phys. Rev. B 66, 085336 (2002)), the Green's function linear response reads: $\$\$ \delta G^R(E,\omega) = G^R(E+\hbar\omega)$ (H $\{ac\}+\delta\sigma^R(E,\omega))G^R(E)$ \$\$

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$\$ \cdot G^{(E,\omega)} = G^R(E+\hbar\omega) H_{ac} G^{(E)} + G^{(E+\hbar\omega)} H_{ac} G^A(E) + G^R(E+\hbar\omega) \cdot G^A(E) + G^R(E+\hbar\omega) \cdot G^A(E) + G^R(E+\hbar\omega) G^A(E) + G^R(E+
```

In the self-consistent gain calculation, the 3 last terms are accounted. Indeed, to account for them, the self-energies $\d G^<(E,\omega)$ need to be calculated from $\d G^<(E,\omega)$, requiring a self-consistent loop. This self-consistent Gain calculation is activated by the command

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<Gain>
<GainMethod>1</GainMethod>
...
</Gain>
```

in the input file. On the other hand, in the case of this command option 0 (not recommended in general though much faster), the 3 terms involving self-energies are neglected.

From this Green's function response, the a.c. conductivity is calculated: \$ \sigma(\omega) = \frac{\delta j(\omega)} {\delta F} \\$\$ where the current a.c. response reads \\$\$ \delta j(\omega) = $Tr(G^< J)$ \\$\$

where \$1\$ is the current operator.

Permittivity and gain/absorption

The bulk relative permittivity, or dielectric constant, is assumed to be given by the Lyddane-Sachs-Teller relation:

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\ \left(\frac{r}{\langle r}}(\omega) = \exp[-(\pi_{\pi}) + (\exp[-(\pi_{\pi})]) \right] + (\exp[-(\pi_{\pi})] + (\exp[-(\pi_{\pi})])
```

In the self-consistent gain calculation, the quantity which is actually calculated is the a.c. conductivity \$\sigma(\omega)\$.

The complex relative permittivity which is output is then:

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\ \epsilon_{\text{r}}(\omega) = \epsilon^{\text{bulk}}_{\text{r}}(\omega) - i \frac{\sigma(\omega)}{\omega \epsilon 0} $$
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Finally the gain reads

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\ g(\omega) = -\frac{\text{Re}(\sigma(\omega))} {\epsilon {\text{r}}(\omega)} $$
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